ПAmibia UחIVERSITY
OF SCIEПCE AПD TECHחOLOGY

## FACULTY OF MANAGEMENT SCIENCES

## DEPARTMENT OF ACCOUNTING, ECONOMICS AND FINANCE

| QUALIFICATION: BACHELOR OF ECONOMICS |  |
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| QUALIFICATION CODE: 12BECO | LEVEL: 7 |
| COURSE CODE: ECM712S | COURSE NAME: ECONOMETRICS |
| SESSION: JAN 2019 | PAPER: THEORY |
| DURATION: 3 HOURS | MARKS: 100 |


| SUPPLEMENTARY/ SECOND OPPORTUNITY EXAMINATION QUESTION PAPER |  |
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| EXAMINER(S) |  |
|  | MR EDEN TATE SHIPANGA |
|  | MR PINEHAS NANGULA |
| MODERATOR: | DR R. KAMATI |

## INSTRUCTIONS

1. Answer ALL the questions.
2. Write clearly and neatly.
3. Number the answers clearly.

## PERMISSIBLE MATERIALS

1. PEN,
2. PENCIL
3. CALCULATOR

## Question 1 [25 marks]

WEEKLY FAMILY INCOME $X, \$$

|  | 80 | 100 | 120 | 140 | 160 | 180 | 200 | 220 | 240 | 260 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Weekly family <br> consumption <br> expenditure $Y, \$$ | 55 | 65 | 79 | 80 | 102 | 110 | 120 | 135 | 137 | 150 |
|  | 60 | 70 | 84 | 93 | 107 | 115 | 136 | 137 | 145 | 152 |
|  | 65 | 74 | 90 | 95 | 110 | 120 | 140 | 140 | 155 | 175 |
|  | 70 | 80 | 94 | 103 | 116 | 130 | 144 | 152 | 165 | 178 |
|  | 75 | 85 | 98 | 108 | 118 | 135 | 145 | 157 | 175 | 180 |
|  | - | 88 | - | 113 | 125 | 140 | - | 160 | 189 | 185 |
|  | - | - | - | 115 | - | - | - | 162 | - | 191 |

1. Given the table above compute the following:
(a) The conditional mean
(b) The unconditional mean
2. With proper examples draw a distinction between mathematical and econometric model?
3. State what the abbreviation TSS stands for and briefly explain what message does it convey about regression analysis?
4. Describe the various components of the function $Y_{i}=E\left(Y \mid X_{i}\right)+\mu_{i}$.
5. Given $\sum \hat{\mathrm{u}}_{\mathrm{i}}^{2}=\sum\left(\mathrm{Y}_{\mathrm{i}}-\widehat{\beta}_{1}-\widehat{\beta}_{2} \mathrm{X}_{\mathrm{i}}\right)^{2}$ derive the normal equations and eventually the estimation equations for $\widehat{\beta}_{1}$ and $\widehat{\beta}_{2}$ ?

## QUESTION 2[25 marks]

1. State the two distinct features of the interceptless model.
2. One of the "consequences of error of measurement in the regressand is increased variance of the estimators". Formulate a scenario and provide proof of this statement.
3. Convert the following intrinsically functions into linear equations.
(a) $\quad Y_{t}=e^{\beta_{1}+\beta_{2} X_{t}+u_{t}}$
(b) $\quad Y_{t}=\frac{1}{1+e^{\beta_{1}+\beta_{2} X_{t}+u_{t}}}$
(c) $\quad Y_{t}=\beta_{1}+\beta_{2}\left(\frac{1}{x_{t}}\right)+u_{t}$

## Question 3 [25 marks]

1. Consider a two-variable model where consumption as a regressand and income as a regressor.
(a) Name the parameter that can be used to measure the spread of the values from their expected values?
(b) Suppose, a researcher is interested in measuring the strength of the relationship between consumption and income, name the parameter one can use to quantify this relationship?
2. Assuming a three-variable model $Y_{t}=\alpha_{1}+\alpha_{2} X_{2}+\alpha_{3} X_{3}$, where $\alpha_{2}$ and $\alpha_{3}$ are partial regression coefficients. You have been asked in a job interview to briefly describe the meaning of the two parameters in this context.
3. Given the regression output below answer the questions that follow. Where NFA net foreign asset
Dependent Variable: LNM2 is money supply, both in natural log.
Method: Least Squares
Sample(adjusted): 2006:02 2016:12
Included observations: 155 after adjusting endpoints

| Variable | Coefficien | Std. Error | t-Statistic | Prob. |
| :---: | :---: | :---: | :---: | :---: |
| C | 0.009936 | 0.003298 | 3.012688 | 0.0030 |
| LNNFA | 0.211279 | 0.023192 | 9.110164 | 0.0000 |
| R-squared | 0.351681 | Mean dependent var |  | 0.012806 |
| Adjusted R-squared | 0.347444 | S.D. dependent var |  | 0.050598 |
| S.E. of regression | 0.040874 | Akaike info criterion |  | 3.543841 |
| Sum squared resid | 0.255611 | Schwarz criterion |  | -. 504571 |
| Log likelihood | 276.6477 | F-statistic |  | 82.99509 |
| Durbin-Watson stat | 2.353923 | $\operatorname{Prob}(\mathrm{F}$-statistic) |  | 0.000000 |

(a) Write out the regression equation estimated in this study.
(b) Interpret the estimated function in (a).
(c) Identify the regressors and regressand.
(d) What is the value of the coefficient of determination?
(e) How many parameters are in this model?
(f) What type of regression model is this?
(g) What does the abbreviation OLS stand for?

## QUESTION 4 [25 marks]

Given the following information on weekly family income ( X ) and weekly family consumption ( Y )

| $Y$ | $X$ |
| :--- | :--- |
| 60 | 80 |
| 70 | 100 |
| 84 | 120 |
| 93 | 140 |
| 107 | 160 |
| 115 | 180 |
| 136 | 200 |
| 137 | 220 |
| 145 | 240 |
| 152 | 260 |

1. Estimate the regression line from the given sample observations?
2. Compute the variance of the estimated residuals?
3. Work out the following RSS, ESS, TSS, $\operatorname{var}\left(\hat{\beta}_{2}\right)$ and $\operatorname{se}\left(\hat{\beta}_{2}\right)$ ?

## QUESTION 5 [25 marks]

1. Interpret the intercept and slope coefficients of the following regression. $\hat{Y}_{i}=$ $56.1-1.7 \mathrm{X}_{\mathrm{i}}$ where $\mathrm{Y}=\%$ of vote received by the incumbent president and $\mathrm{X}=$ unemployment rate (in percentage points)
2. Interpret the intercept and slope coefficients of the following regression. $\ln \hat{Y}_{i}=$ $3.5+1.35 \ln X_{i}$ where $Y=G N P$ (in millions of $\$$ ) $X=$ Government spending (in mills. of dollars)
3. Interpret the intercept and slope coefficients of the following regression. $\hat{Y}_{i}=-$ $1.8+45.8 \ln X_{i}$ where $Y=$ inflation rate (\%) and $X=$ wage rate (in $N \$$ )
4. Interpret the intercept and slope coefficients of the following regression. In $\hat{Y}_{i}=$ $4.1+0.05 \mathrm{~T}$ where $\mathrm{Y}=\mathrm{GDP}$ (in mill. of dollars) and $\mathrm{T}=$ time trend ( $\mathrm{T}=1,2,3, \ldots$ representing years)
5. Interpret the intercept and slope coefficients of the following compound growth rate of $\ln \hat{Y}_{i}=4.1+0.05 \mathrm{~T}$ where $\mathrm{Y}=\mathrm{GDP}$ (in mill. of dollars) and $\mathrm{T}=$ time trend ( $\mathrm{T}=1,2,3, \ldots$ representing years)
6. Write the expression that represents a regression that estimate the average salaries of two group of teacher (a graduate and none graduate) interpret it and graph it.
